

Estimating General Equilibrium Spillovers of Large-Scale Shocks

Summary Slides
Kilian Huber

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- Alternative: directly estimate spillovers using multi-layered variation

Related Literature

- Few studies in macro and finance directly estimate spillovers
Dupor and McCrory 2018; Huber 2018; Bernstein et al. 2019; Auerbach et al. 2020; Gathmann et al. 2020; Helm 2020; Verner and Gyöngyösi 2020; Conley et al. 2021; Berg et al. 2021; Mian et al. 2022
- Methods tailored to labor and RCTs (“closed economies”, Egger et al.)
Ammermueller and Pischke 2009; Epple and Romano 2011; Sacerdote 2011; Angrist 2014; List et al. 2019

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Ammermueller and Pischke 2009; Epple and Romano 2011; Sacerdote 2011; Angrist 2014; List et al. 2019
- This paper: framework and advice tailored to macro and finance
 - multiple spillover types
 - nonlinearities
 - mismeasurement (Ammermueller and Pischke 2009; Angrist 2014)
 - policy multipliers

This Paper

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5. Practical advice

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- Define types of spillovers to be estimated, e.g., across firms/households in
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- Application: effect of credit cut on firms, both directly affected firms and unaffected firms in same region and product market.

Framework

- Linear model:

$$y_i = \beta x_i + \sum_{j \neq i, \text{reg.}} \gamma^j x_j + \sum_{k \neq i, \text{ind.}} \lambda^k x_k + \alpha + \epsilon_i$$

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- γ^j = spillover = change in y_i due to treatment of firm j (same region)
- λ^k = spillover = change in y_i due to treatment of firm k (same industry)

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- Assume exogeneity, so biases not driven by endogeneity or “reflection problem”: $E(x_i \epsilon_i) = 0$
- Assume systematic variation across groups:

$$x_i = u_{r(i)} + u_{s(i)} + \nu_i$$

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- More on how to calculate dollar multipliers etc. in paper.

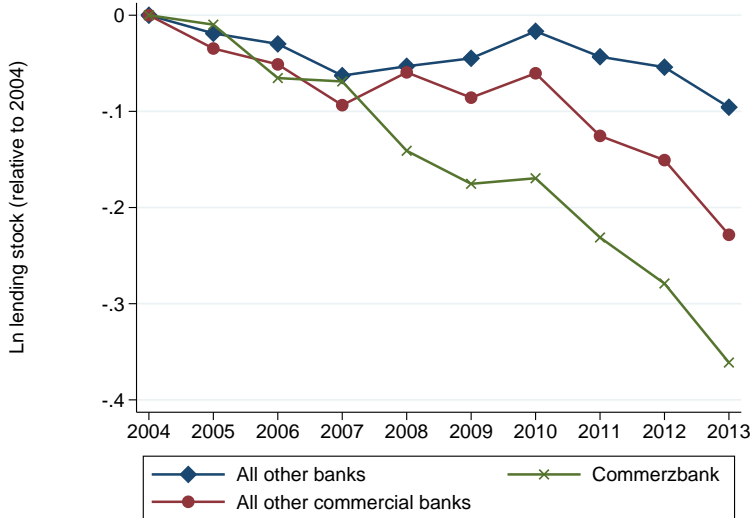
Application: Credit Cut

- A German bank (Commerzbank) cuts lending due to international losses (Huber 2018).
- Some firms depend on this bank for credit.

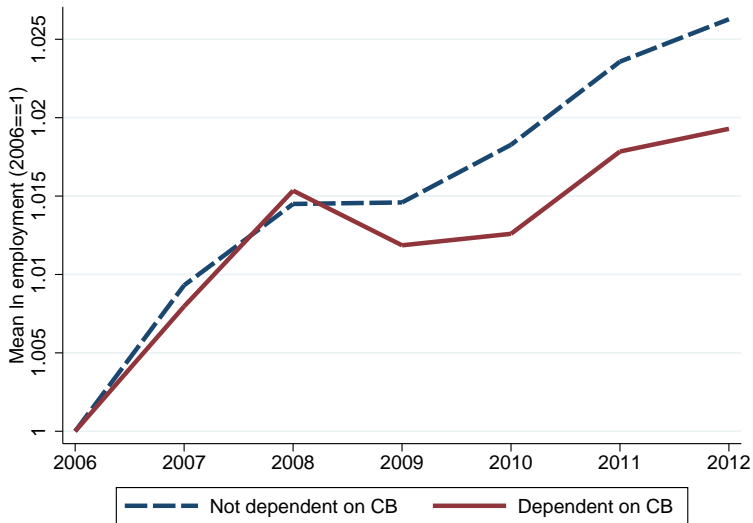
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- Some firms depend on this bank for credit.
- Treatment: Indicator for direct dependence on the bank.
- Research question: amplification or dampening through spillovers?

Credit cut by Commerzbank



Direct Employment Effect



Product Market Spillovers

- IO economists write theories about product markets: demand versus technology spillovers.
- Test by constructing product market leave-out mean (industry for tradable and industry-region for non-tradables).
- Estimate:

$$y_i = \beta x_i + \lambda \overline{x_{s(i)}} + \alpha + u_i$$

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- There are other potential spillovers, e.g., region. But region and industry means are uncorrelated. So no OVB?
- No, cannot take spillover estimate at face value.
- There will be mechanical bias if a true spillover is excluded, even if uncorrelated to other spillover.
- Regional spillovers operate through demand versus agglomeration spillovers.

Add Regional Spillover

Coefficient on x_i	-0.030*** (0.007)	-0.027*** (0.007)
Coefficient on $\overline{x_{s(i)}}$	-0.030* (0.018)	-0.015 (0.018)
Coefficient on $\overline{x_{r(i)}}$		-0.114** (0.051)

Sectors in sample	All sectors	
Observations	45,252	45,252

Understanding Mechanical Bias

- True model:

$$y_i = \beta x_i + \gamma \overline{x_{r(i)}} + \lambda \overline{x_{s(i)}} + \alpha + \epsilon_i$$

- Excluded regional term correlated with direct effect, so all coefficients biased.

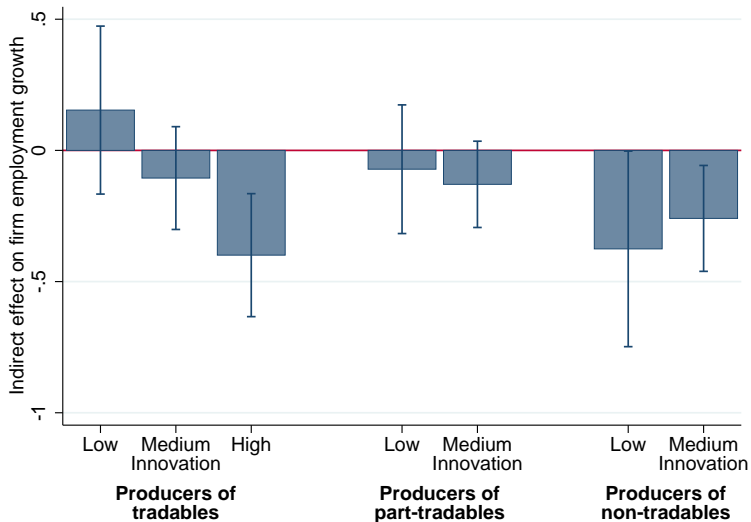
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- Suggestions:
 - if observed, include other spillover types
 - IV
 - heterogeneity in spillovers using theory

Heterogeneous Regional Spillover



Heterogeneous Regional Spillover

-0.031**

(0.013)

-0.026***

(0.009)

-0.045

(0.031)

-0.007

(0.024)

-0.213***

(0.077)

-0.067

(0.055)

Non-tradable and
high R&D

14,810

Tradable and
low R&D

30,442

Mechanical Bias due to Mismeasurement

- Incorrectly specified regressors generate mechanical bias:
 - direct effect is nonlinear, but direct treatment is measured using linear regressor
 - measurement error in direct treatment
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- For exposition, introduce measurement error in direct treatment
- Size of “high” error calibrated using Bound and Krueger (1991) error in earnings growth.

Measurement Error

Coefficient on x_i^*	-0.027*** (0.007)	-0.023*** (0.006)	-0.024*** (0.006)	-0.009 (0.006)
Coefficient on $\overline{x_{r(i)}}^*$	-0.123** (0.050)	-0.155*** (0.054)	-0.160*** (0.058)	-0.256*** (0.086)

Measurement error	None	Low	Medium	High
Sectors in sample		All sectors		
Observations	45,252	45,252	45,252	45,252

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- Individual measurement error gets averaged away in leave-out mean.
- Less error in leave-out mean than in direct effect.
- True direct effect erroneously loads onto spillover coefficient.
- Analytical derivation for biases in paper.

Little Heterogeneity with ME

-0.021**

(0.010)

-0.004

(0.007)

-0.346***

(0.128)

-0.214**

(0.094)

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Mismeasurement Solutions

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- Same intuition for nonlinear effect, very relevant for finance, e.g., borrowing and liquidity constraints.

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- Bank debt: Direct effect = 0.47 mio decline at average firm.
- Employment: Total effect = 10 jobs.
- Undo direct effect at 0.47 mio per firm, get 10 jobs in region.
- Provide 100k USD in debt, get 1.4 jobs.
 - Know only direct effect: would estimate 0.4 jobs.
 - Know only region effect: don't know how to target direct firms.

Recommendations

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- 5. Identify theoretical mechanisms driving spillovers.
 - regional: demand and agglomeration effects
 - sectoral: competition and productivity
 - cross region: trade, migration, capital mobility, and aggregate policy

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- 6. Estimate heterogeneous spillovers as suggested by theory

Conclusion

- Macro shocks affect firms/households through many complex GE spillover channels.
- Need to know GE channels for modeling and policy → estimating spillovers is potentially powerful .
- More potential applications sketched in paper, ranging from sectoral, labor market, and country-level spillovers.
- Most challenging: estimating country spillovers requires exogenous country variation.
 - fiscal spending due to wars (Ramey 2019)
 - foreign policy (Jiménez et al. 2012)
 - political upheavals (Fuchs-Schündeln 2008)
 - idiosyncratic policy (Romer and Romer 2004)